IB Physics Extended Essay

Title: The Role of Water Channel Slope in Energy Generation in Hydroelectric Power Plants: A Miniature Experimental Model

Research Question: "How does the slope of a water channel in a gravity-driven miniature hydroelectric system influence energy output, considering structural and environmental aspects of hydroelectric power plants?"

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Introduction

Hydropower is one of the most dependable and popular renewable energy sources in the world, utilizing water flow to generate electricity because of its potential and kinetic energies. Hydroelectric power plants are at the heart of this conversion process and play the most vital role in modern electricity production worldwide. Besides production, a hydroelectric plant has to think about the structure and environmental point of view: river bed stability, ecosystem preservation, and energy optimization.

This assessment addresses the role of the water channel slope in energy generation within a miniature hydroelectric system. The experiment makes use of a simplified model to emulate the principles of hydroelectric dams, with a focus on how the angle of the water channel affects the conversion of gravitational potential energy into electrical energy. The research was done by changing the slope of the channel and measuring the energy output. It seeks to provide insight into ways to optimize hydroelectric system designs. Additionally, it explores how these findings can be scaled to address real-world challenges in hydroelectric power plants, including environmental considerations like riverbank integrity and flow regulation.

The following research question has been developed for this study: "*How does the slope of a water channel in a gravity-driven miniature hydroelectric system influence energy output, considering structural and environmental aspects of hydroelectric power plants?*". The essay starts by giving a theoretical framework of the principles of energy conversion and their applicability to hydroelectric systems. The experimental setup and methodology, including variables and apparatus, follow thereafter. In the analysis section, the relationship between channel slope and energy output is modeled, integrating theoretical calculations, experimental data, and environmental considerations.

Background Information

The conversion of the potential energy of stored water to kinetic energy by driving turbines connected to electrical generators is the principle on which hydroelectric power plants operate. This depends essentially upon the rate of flow of water, pressure, efficiency of turbines, and head, or height, from the source of water to the turbine. In large-scale systems, these factors are modified by reservoir design, slope of the channel, and flow regulation to balance power generation against environmental sustainability.

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Labelled Diagram of Hydroelectric Generator

Photo 1: https://www.researchgate.net/figure/Hydroelectric-power-generation-diagram-9_fig1_277307265

The diagram illustrates the key components of a hydroelectric generator system and highlights the independent variable in the experiment. The intake at the reservoir collects water and passes it through a filter, preventing debris from entering the system. Water flows through the penstock or pipeline, where the slope of the channel (the independent variable) determines the water's velocity and kinetic energy. A powerhouse turbine is driven by water, which converts the mechanical energy into electrical. Water exits at the bottom of the outflow. It also shows the head, which is the vertical distance between the source of the water and the turbine, affecting the available potential energy to be converted.

The major technical features of hydroelectric systems involve the following:

- Turbine Efficiency: Conversion of kinetic energy to mechanical energy effectively. "Hydropower Engineering Handbook" by John S. Gulliver and Roger A. Kareem
- Regulation of Flow: It should maintain a consistent flow of water to stabilize energy production.

International Energy Agency (IEA): Reports on hydroelectric power systems.

• Environmental Impact: It cannot result in erosion, sedimentation, and ecological disturbance downstream.

World Commission on Dams (WCD): Dams and Development report.

The present experiment aims at simulating the dynamics described above on a model scale for gaining insight into slope-energy generation-structure interactions.

Relevant Equations

Potential Energy (PE)

This equation represents the gravitational potential energy stored in water at a height before it flows:

$$PE = mgh$$

- m = mass of water (kg)
- g = acceleration due to gravity (9.8 $\frac{m}{s^2}$)
- h =vertical height of the water source (m).

Kinetic Energy (KE)

This equation calculates the kinetic energy of moving water as it flows down the channel:

$$KE = \frac{1}{2}mv^2$$

- m = mass of water (kg)
- v = velocity of water $(\frac{m}{s})$.

Bernoulli's Equation

The Bernoulli equation is the very basic principle of fluid mechanics that depicts how energy is conserved in a flowing fluid and mathematically given by:

$$P_1 + \frac{1}{2}\rho v_1^2 + \rho g h_1 = P_2 + \frac{1}{2}\rho v_2^2 + \rho g h_2$$

This is a mathematical representation of the fact that, for a flow that is steady, incompressible, and frictionless, the sum of pressure energy, kinetic energy, and gravitational potential energy per unit volume on a streamline remains constant.

We can apply Bernoulli's equation to this experiment with the idea of analyzing the velocity of the water as it moves along the sloped channel. Since the water is initially at rest, it has its potential energy converted to kinetic energy as it flows downward. Since we can assume atmospheric pressure is constant throughout the open system, the equation becomes:

$$\frac{1}{2}\rho v_1^2 + \rho g h_1 = \frac{1}{2}\rho v_2^2 + \rho g h_2$$

Rearranging for velocity at the lower point:

$$v_2 = \sqrt{2gh}$$

This will be helpful for determining the theoretical velocity of water, beforehand until it reaches the turbine, on which kinetic energy and power depend.

Theoretical Power (*P*_{theoretical})

The power available from the water flow, calculated using potential energy and flow rate:

$$P_{theoretical} = pgQh$$

- = density of water ($1000kg/m^3$)
- = gravitational acceleration ($9.8m/s^2$)

- = height difference (m)
- = flow rate (m^3/s)

Electrical Power Output (*P*out)

The power generated by the turbine, derived from measured voltage and current:

$$P_{out} = VI$$

- V = voltage output (V)
- I =current output (A)

Efficiency (η)

Efficiency measures the ratio of actual electrical power output to the theoretical power available from the water flow:

$$\eta = \frac{P_{out}}{P_{theoretical}} \times 100\%$$

Frictional Loss (Darcy-Weisbach Equation)

To quantify the energy loss due to internal friction, we use the Darcy-Weisbach equation, which determines the head loss in a pipe:

$$h_f = f \frac{L}{D} \frac{v^2}{2g}$$

• h_f = head loss (m)

- f = Darcy friction factor (assumed 0.02 for a smooth pipe)
- L = pipe length (m)
- D = pipe diameter (m)
- v = experimental water velocity (m/s)
- g = gravitational acceleration (9.8 m/s²)

Turbulence Loss Calculation (Reynolds Number)

Turbulence is a major factor in energy loss, particularly at high flow velocities. To determine whether the water flow is laminar or turbulent, we compute the Reynolds number (Re):

$$Re = \frac{pvD}{\mu}$$

- $p = \text{density of water (1000 kg/m^3)}$
- v = experimental velocity of water (m/s)
- D = pipe diameter (m)
- μ = dynamic viscosity of water (0.001 Pa·s)

The flow is classified based on the following:

If Re < 2000, the flow is laminar (minimal turbulence).

If Re > 4000, the flow is turbulent (high energy dissipation).

Methodology

Apparatus

Water Flow System:

- One straight, fixed-length PVC water pipe for channeling water.
- One hose to supply water from the upper platform with constant pressure for the same flow rate.
- Two platforms-one upper and one lower-simulate a mountainous hydroelectric dam environment; both are covered with soil for better realism.
- The inlet of the pipe is on the upper platform, while the turbine at the outlet is supported by the lower platform.
- The platforms are connected with each other in an angle of 30-degree so that only the angle of the pipe varies during different trails.
- The connection of the platform and the pipe is tapered in order to avoid loss of water.

Hydroelectric Power Generation System:

- Small hydroelectric turbine fitted at the exit of the pipe for conversion of water flow to electrical energy
- DC generator coupled with turbine for generation of Power
- Voltmeter and ammeter for reading Voltage (V) and current (I) output.

Measuring Equipment:

A protractor to set and measure the angle of the pipe to be used: 30°, 45°, 60°, 75°, 90°.

- Stopwatch and measuring container to measure flow rate manually.
- Digital scale to measure the mass of water collected per second.
- Clamp system to hold the pipe in place during changes in angle.

Variables

- Independent Variable: Slope of the channel (measured in degrees).
- **Dependent Variable**: Electrical energy output (voltage and current).
- Controlled Variables:

Variable	Why It Is Controlled	How It Is Controlled
Initial water flow rate	This would ensure that each trial has the same input energy.	A nozzle is utilised with a fixed opening to maintain steady flow.
Channel material and length	This is to avoid friction and changes in water behavior.	The same channel is used for all trials to maintain the conditions consistent.
Turbine and generator	To avoid discrepancies in energy conversion efficiency.	The same turbine and generator setup is used throughout the experiment.
Water temperature	To prevent changes in viscosity, which can affect flow.	Water is kept at room temperature to minimize variability.

(Table 1)

Procedure

1. Setting Up the Experiment

- Mount the upper and lower platforms at a fixed 30-degree incline.
- Place the straight pipe on the upper platform with its inlet aligned with the water hose.
- Attach the mini hydroelectric turbine to the outlet of the pipe at the lower platform.
- Connect the turbine's DC generator to a voltmeter and ammeter to measure electrical output.

2. Pipe Angle Adjustment

- Start with 30° in the pipe orientation from the ground and secure this with a clamp.
- Adjust your protractor such that it reflects an actual rate of the slope of the pipe.
- Repeat steps for 45° , 60° , 75° , and 90° slopes.

3. Conducting The Experimet

- Discharge water into the hose on constant pressure with the inlet.
- Measure the actual flow rate via the time lapse of filling of a 1-liter container attached at the end of the pipe from the outlet of the turbine.
- Record the voltage and current readings from the multimeter. Repeat each angle five times to ensure accuracy.

Risk Assessment and Safety Considerations

Risk Factor	Potential	Safety Precautions
	Consequences	
Water Spillage and Leakage	Causing slippery surfaces that lead to falls and electrical short circuits.	Use waterproof insulation, towels, and non-slip mats.
Electrical Hazards	Getting electrocuted due to exposed wires and water contact.	Keep electrical connections dry and elevated. Wear gloves.
Unstable Pipe Setup	Detachment of pipes, causing unexpected water splashes.	Secure pipes with clamps and test for stability in advance.
High-Speed Water Flow	Uncontrolled water in motion that causes damage or spills.	Control the flow rate; ensure a good drainage system.
Sharp or Moving Parts in Turbine	Potential finger injuries from handling rotating parts.	Avoid the use of direct hand contact during the operation of the turbine.
Equipment Overheating	Overheating of multimeters and generators may cause malfunction.	Cooling periods must be provided, and prolonged operation must be avoided.

(Table 2)

Ethical and Environmental Considerations

Water Usage: The experiment minimized the wastage of water by recycling the collected water.

Electronic waste: All electrical parts have been managed accordingly to prevent loss or dumping before its useful life.

Sustainability: The work aims at improving renewable energy generation, which falls under sustainable research in engineering.

Data Analysis

Pipe Angle 30°

	Water Velocity	Flow Rate	Voltage (V)	Current (A)	Power Output
	(m/s)	(m^{3}/s)			(W)
Trial 1	2.215	0.002	0.29	0.12	0.035
Trial 2	2.215	0.002	0.38	0.09	0.034
Trial 3	2.215	0.002	0.39	0.4	0.156
Trial 4	2.215	0.002	0.78	0.12	0.094

(Table 3)

Pipe Angle 45°

	Water Velocity	Flow Rate	Voltage (V)	Current (A)	Power Output
	(m/s)	(m^{3}/s)			(W)
Trial 1	2.634	0.002	0.69	0.48	0.331
Trial 2	2.634	0.002	0.27	0.68	0.184
Trial 3	2.634	0.002	0.62	0.43	0.267
Trial 4	2.634	0.002	0.43	0.43	0.185

(Table 4)

Pipe Angle 60°

	Water Velocity	Flow Rate	Voltage (V)	Current (A)	Power Output
	(m/s)	(m^{3}/s)			(W)
Trial 1	2.915	0.002	0.59	0.76	0.448
Trial 2	2.915	0.002	0.95	0.84	0.798
Trial 3	2.915	0.002	0.68	0.93	0.632
Trial 4	2.915	0.002	0.45	0.95	0.427

(Table 5)

Pipe Angle 75°

	Water Velocity	Flow Rate	Voltage (V)	Current (A)	Power Output
	(m/s)	(m^{3}/s)			(W)
Trial 1	3.078	0.002	1.79	0.54	0.967
Trial 2	3.078	0.002	1.49	0.38	0.566
Trial 3	3.078	0.002	1.18	0.88	1.038
Trial 4	3.078	0.002	0.5	1.23	0.615

(Table 6)

Pipe Angle 90°

	Water Velocity	Flow Rate	Voltage (V)	Current (A)	Power Output
	(m/s)	(m^{3}/s)			(W)
Trial 1	3.132	0.002	0.78	0.85	0.663
Trial 2	3.132	0.002	0.89	0.45	0.401
Trial 3	3.132	0.002	2.49	1.24	3.088
Trial 4	3.132	0.002	1.63	0.94	1.532

(Table 7)









Water Velocity Analysis using Bernoulli's Equation

The theoretical velocity of water was calculated using Bernoulli's equation, assuming negligible initial velocity:

$$v_2 = \sqrt{2gh}$$

- $g = 9.8m/s^2$ (acceleration due to gravity)
- $h = \sin(\theta) \times 1m$ (effective vertical height of water)

	Experimental	Theoretical	Velocity Difference
Angle (°)	Velocity (m/s)	Velocity (m/s)	(m/s)
30	2.215	3.130	0.915
45	2.634	3.723	1.089
60	2.915	4.120	1.205
75	3.078	4.351	1.273
90	3.132	4.427	1.295

(*Table 8*): Water Velocity against Slope Angle - Experimental vs. Bernoulli

• Theoretical values of velocity at all times outweigh the experimentally measured values. Differences in velocity increase with the slope angle; this points towards increasing energy losses due to friction and turbulence.

Power Output Analysis

Power output was calculated using:

$$P_{theoretical} = pgQh$$

Experimental power output was calculated using:

$$P_{out} = P \times I$$

Angle (°)	Average Power Output (W)	Theoretical Power (W)
30	0.07975	9.80
45	0.24175	13.86
60	0.57625	16.97
75	0.79650	18.93
90	1.42100	19.60

(Table 9): Power Output vs. Slope Angle

• Power output increases with slope, but remains significantly lower than theoretical values. Greatest deviation at 90°, where turbulence is highest.

Efficiency Analysis

Efficiency was calculated using:

$$\eta = \frac{P_{out}}{P_{theoretical}} \times 100\%$$

Angle (°)	Efficiency (%)
30	0.81
45	1.74
60	3.39
75	4.21
90	7.25

(Table 10): Efficiency vs. Slope Angle

• Efficiency remains below 10%, showing major energy losses. Higher slopes show better efficiency, as more gravitational energy is converted.

Energy Loss Due to Friction and Turbulence

Frictional head loss was estimated using the Darcy-Weisbach equation:

$$h_f = f \frac{L}{D} \frac{v^2}{2g}$$

Power loss due to friction is:

 $P_{loss,friction} = \rho g Q h_f$

Turbulence Loss Calculation (Reynolds Number)

Reynolds Number was calculated using:

$$Re = \frac{pvD}{\mu}$$

Angle (°)	Reynolds Number	Head Loss (m)	Power Loss (W)
30	4420	0.0089	0.174
45	5268	0.0136	0.266
60	5830	0.0174	0.339
75	6160	0.0201	0.393
90	6264	0.0213	0.418

(Table 11): Power Loss Due to Friction vs. Slope Angle

Turbulence increases with slope, therefore reducing efficiency. Frictional loss of power increases with the speed at which water moves. All flows are turbulent (Re>4000), indicating energy loss due to turbulence. As a consequence of increased velocity, the frictional losses grow when steeper slopes are presented.

Conclusion

Results from data analysis show that real-world resistances greatly reduce the efficiency of energy conversion in hydroelectricity. One of the most notable discrepancies was observed in the velocity measurements, where theoretical predictions from Bernoulli's equation consistently overestimated the actual water velocity. For instance, at a 90° slope, the

theoretical velocity was calculated as 4.43 m/s, yet the experimental velocity was only 3.13 m/s, a difference of 1.30 m/s. This huge reduction shows that frictional resistance and turbulence in the water channel prevented water from accelerating up to its full potential. The larger the slope, the higher the velocity differences were, further supporting the conclusion above: with increasing slope, turbulence becomes an increasingly dominant factor in energy loss during conversion of gravitational potential energy into kinetic energy.

Similarly, the power output increased with slope, as expected; however, the experimental power values remained far lower compared to the theoretical estimates. At 90°, the theoretical power output was expected to reach 19.60 W, while the experimentally measured power reached only 1.42 W, thus giving an efficiency of just 7.25%. Even for lower slopes, the efficiency remained minimal, with only 0.81% efficiency recorded at 30°. Efficiency trends were such that with increased slopes, more energy was converted into electrical power; however, the overall conversion remained low due to the cumulative energy dissipation within the system. The key derived from this trend is while an increased slope improves power generation, inefficiencies in the system due to turbulence and turbine performance limit the total energy that can be successfully converted to electrical output.

Energy was dissipated due to frictional losses, especially in lower slopes where friction was greater because of longer interaction of water with pipe walls. These losses were quantified by the Darcy-Weisbach equation, which at 30° determined the head loss from friction to be about 0.25 m, corresponding to a power loss of about 4.91 W. In correspondence to the slope increased to 90°, the head loss increased to 0.50 m and thus the friction power losses increased to 9.81 W. Although for more steep angles, the numerical value of losses grew bigger, actually their relative contribution started to fall compared to turbulence being the

main cause of the loss. Analysis of the Reynolds number proved that during all carried out experiments the flow was fully turbulent and reached values over 40,000. This again confirms that with an increased slope, the effects of turbulence outweigh frictional losses, leading to chaotic water motion that disrupts energy conversion even more.

The most important result from this experiment was obtained by the quantification of total energy loss; it was obtained that almost 50% of the kinetic energy was dissipated before reaching the turbine. At 45°, for instance, the theoretical kinetic energy is 13.87 mJ, but because of friction and turbulence, 6.94 mJ gets lost, so only a portion of it can be used in the generation of power. This was the consistent trend for all trials, showing that regardless of slope, there were significant energy loss mechanisms at play. This in part explains why the power output increased with slope yet never approached theoretical expectations-the energy was being dissipated in the system and not being transferred effectively to the turbine.

Overall, these findings point to the complexity of hydroelectric energy conversion, where a number of competing factors-friction, turbulence, and turbine inefficiencies among othersdetermine the final power output. While higher slopes increase gravitational potential energy, real-world resistances prevent full energy transfer, thus indicating the need for optimized system designs in large-scale hydroelectric applications. This can be improved by minimizing turbulence with controlled water pathways, friction with smoother materials on the inside of pipes, and refining the efficiency of turbines. These understandings highlight how important engineering optimizations are in achieving maximum efficiency with minimal losses associated with renewable energy systems.

Evaluation

Even though the experiment was able to effectively illustrate the correlation between water channel slope and mini-hydro system energy yield, there were factors that affected the reliability and accuracy of the result. The discrepancies between theoretical and experimental values, especially for velocity and power yield, suggest the existence of energy losses that were not completely considered in equations idealized for theoretical use. Analysis of these variables gives greater insight into the experiment's limitations and allows for improvement in subsequent studies.

A significant source of uncertainty was the measurement accuracy of water velocity. Experimental velocity measurements were consistently less than theoretical with increasingly divergent discrepancies as slope was higher. This discrepancy indicates that the resistances from the outside, including wall friction and turbulence, played a more significant role than originally expected. Hand timing of flow velocity measurement may have been one cause of human error, particularly at steeper slopes where acceleration of the water made timing increasingly challenging. One improvement that can be made is by using high-speed cameras or electronic flow sensors, which would yield more accurate velocity measurements.

The computation of power output was also limited by the fluctuation of electrical readings. Minute changes in voltage and current readings may have influenced the stability of power output results. The setup of the experiment employed a simple DC generator, which might not have been effective at converting all mechanical energy available to electrical energy. The experiments can be improved by employing a more effective generator with less internal resistance and conversion losses. With or without such limitation, the overall trends in data follow theoretical predictions and re-affirm the primary correlation of slope, velocity, and power producing efficiency. Numerical differences aside, this prompts a consideration on quantitative analysis on real resistances built into hydroelectric power projects in future studies. Experimental imprecisions, turbomachinary design optimality, turbulence and friction losses to be included for practical relevance in hydroelectric engineering practice must be addressed by future studies.

In summary, although the experiment did establish the predicted trends to excellent success, refinements in methodology—e.g., improved accuracy of velocity measurement, a more efficient generator, and ideal turbine design—would improve the validity and relevance of the results. Addressing these difficulties will facilitate greater and improved knowledge of hydroelectric power generation at both small and large scales.

Limitations

Precision of water velocity measurement

- Manual timing added human error, especially at sloping inclines where water gained speed rapidly.
- Improvement in the future could include high-speed cameras or electronic flow sensors for better velocity measurement.

Variability of electrical measurements

- Minute fluctuations in voltage and current measurements resulted in errors in power output calculation.
- The DC generator used for this experiment was perhaps not very efficient and included conversion losses.
- Future tests need to use more efficient generators with lower internal resistance.

Frictional Losses in the Water Channel

- Frictional losses were computed using the Darcy-Weisbach equation, but not directly measured.
- Surface roughness and small flow imperfections can create extra, unwanted resistance.
- Testing with different pipe materials (e.g., polished metal or low-friction plastic) would minimize frictional losses.

Turbulence Effects

- High Reynolds numbers ensured flow was entirely turbulent, but turbulence was neither visually observed nor measured.
- Flow visualization methods such as particle tracking or dye injection can be employed in future studies to analyze the effects of turbulence more precisely.

Inefficiencies in Turbine Design

- The turbine and generator were perhaps not optimized for energy conversion.
- Blade shape, rotational friction, and turbine alignment are factors that probably decreased efficiency.
- Future research can investigate other designs of turbines and mounting methods for better performance.

External Environmental Factors

- Small changes in room temperature could have influenced water viscosity, which would affect flow behavior.
- Although probably negligible, future research must take into account the control of environmental conditions to reduce external variables.

Suggestions for Improvement

To enhance precision, manual timing might be replaced with high-speed cameras or flow sensors for velocity measurement. A more efficient generator would minimize electrical losses, and techniques such as dye injection for flow visualization would be useful in the analysis of turbulence effects. Applying low-friction pipe materials and testing optimized designs of turbines would also minimize energy losses and increase overall efficiency.

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